

Desired Stage Length	3.05 in	77.47 mm
Desired Stage Overlap (when retracted)	0.05 in	1.27 mm
Desired Stroke Length	10 in	254 mm
Thread Overlap	0.25 in	6.35 mm
Stop Flange Length	0.25 in	6.35 mm
Effective Stage Length	2.55 in	64.77 mm
Minimum Required Stages	5 stages	
Actual Stroke Length	10.2 in	259.08 mm
Actual Retracted Length	3.3 in	83.82 mm
Smallest Possible Stage (Thread OD)	0.5 in	12.7 mm
Minimum Acceptable Wall Thickness	0.1 in	2.54 mm
Threads Per Inch	20 tpi	0.787402 tpm
Thread Height	0.027063 in	0.687408 mm
Additional Stop Flange Width	0.025 in	0.635 mm
Stop Flange Clearance	0.05	1.27
Stage 1 Diameter (smallest)	0.55 in	13.97 mm
Stage 2 Diameter	0.8 in	20.32 mm
Stage 3 Diameter	1.05 in	26.67 mm
Stage 4 Diameter	1.3 in	33.02 mm
Stage 5 Diameter	1.55 in	39.37 mm
Stage 6 Diameter	in	0 mm
Stage 7 Diameter	in	0 mm
Stage 8 Diameter	in	0 mm
Stage 9 Diameter	in	0 mm
Stage 10 Diameter	in	0 mm

*when extended*

There are two main types of errors that I anticipate encountering in this mechanism: positioning errors (from the non-perfectness of the screw actuator) and twisting errors (from the torque induced by the rotation of the screw actuator).

The two big positioning errors I am concerned with are:

1. Gravity-induced "sag" Abbe errors in the z-axis from small dimensional differences in the mating threads (at each stage)
2. Backlash or "slop" errors in the x-axis from small dimensional differences in the mating threads (at each stage)

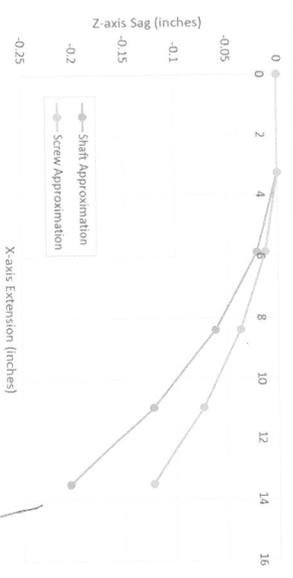
The big twisting error I am worried about is:

1. Roll errors about the x-axis if the screw torque overcomes the rotational/torsional stiffness of the shell (Concept #1) or is mismatched to torque produced by the opposite screw actuator (Concept #2)

**Sag Errors At Full Extension (negative z-axis)**

Number of Sag Joints	Male-Female Diameter Difference (screw approx.)	Effective Diameter Difference (screw approx.)	Sag Per Stage (worst case - shaft approx.)	Sag Angle (worst case - shaft approx.)	Total Sag (worst case - shaft approx.)	Sag Per Stage (screw approx.)	Sag Angle (screw approx.)	Total Sag (screw approx.)
4 joints	0.002 in	0.0012 in	0.0204 in	0.458371 degrees	0.08346 in	0.01224 in	0.275021 degrees	0.04986 in
	0.0508 mm	0.03048 mm	0.51816 mm	0.008 rad	2.07264 mm	0.3109 mm	0.0048 rad	1.24358 mm
<b>Figure</b>	<b>Biggest Stage</b>	<b>Next Smallest</b>	<b>..</b>	<b>..</b>	<b>..</b>	<b>..</b>	<b>..</b>	<b>..</b>
1	0.008000085	2.549918	-0.0204	5.849918	8.399592	-0.0612	0.014400055	2.549736
2	0.016000171	2.549674	-0.040798694	8.399592	10.94886	-0.12239	0.019200074	2.54953
3	0.024000256	2.549266	-0.061194778	10.94886	13.49755	-0.20398	0.04896	13.49912
4	0.032000341	2.548894	-0.081586944	13.49755	16.04711	-0.28557	0.07872	16.04868
5	..	..	..	..	..	..	..	..
6	..	..	..	..	..	..	..	..
7	..	..	..	..	..	..	..	..
8	..	..	..	..	..	..	..	..
9	..	..	..	..	..	..	..	..

This is the smallest segment, so the worst case for bending



So, compared to the sag errors, the bending errors are insignificant

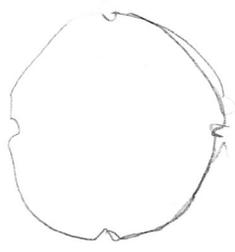
So, compared to the sag errors, the bending errors are insignificant

**Bending Errors (negative z-axis)**

Tube OD	Wall Thickness	Moment of Inertia	Length	Force Applied	Elastic Modulus (6061 Aluminum)	Mass density (6061 Aluminum)	Stiffness (k) (6061 Aluminum)	Deflection (δ) (6061 Aluminum)	Mass (6061 Aluminum)	Resonant Frequency (6061 Aluminum)	Elastic Modulus (304 Stainless Steel)	Mass density (304 Stainless Steel)	Stiffness (k) (304 Stainless Steel)	Deflection (δ) (304 Stainless Steel)	Mass (304 Stainless Steel)	Resonant Frequency (304 Stainless Steel)
0.55 in	0.35 in	0.1 in	3.3 in	10 N	68900 N/mm <sup>2</sup>	2.7E-06 kg/mm <sup>3</sup>	8.77776 N/mm	4.49E-05 in	0.04541 lbs	3282.02 Hz	200000 N/mm <sup>2</sup>	8E-06 kg/mm <sup>3</sup>	25.47917 N/mm	1.55E-05 in	0.134552 lbs	3248.51 Hz
0.35 in	0.1 in	2.54 mm	83.82 mm	25008.4 mm <sup>4</sup>	8.77776 N/mm	1.339243 um	8.77776 N/mm	0.00114 mm	0.02064 kg	3282.02 Hz	200000 N/mm <sup>2</sup>	8E-06 kg/mm <sup>3</sup>	25.47917 N/mm	1.55E-05 in	0.134552 lbs	3248.51 Hz

but this is a huge overestimate

seems like quite a lot of deflection by now overlap - precedence issues



repeatable? might be fine or use shim

**Slop Errors (± x-axis)**

Number of Sag Joints	4 joints		
Male-Female Diameter Difference	0.002 in		0.0508 mm
Max Possible Slop Per Joint	0.001155 in		0.029329 mm
Maximum Total Slop	0.004619 in		0.117318 mm

*Can I see female's behind this  
 4 (51 variants) + Abbe error result from  
 dimensional clearance*

**Shell Twist Errors (roll about x-axis)**

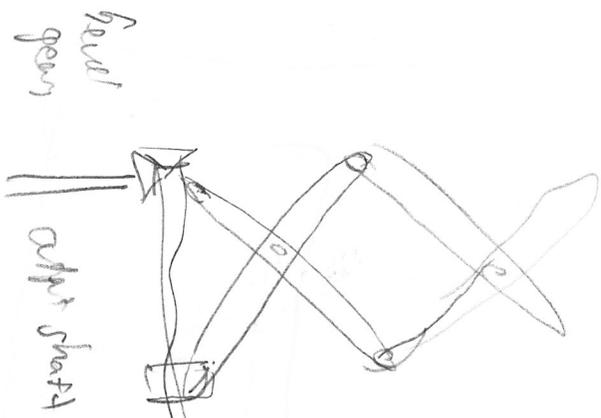
Motor Pull-In/Out Torque		0.3 Nm	
Max Possible Shell Diameter	2.5 in		0.0635 m
Force Felt by Shell At Edge		4.724409 N	
Shell Stage Length	3.05 in		0.07747 m
Shell Stage Wall Thickness	0.025 in		0.000635 m
Shell Inner Diameter	2.45 in		0.06223 m
Polar Moment of Inertia (J)	0.297714 in <sup>4</sup>		1.24E-07 m <sup>4</sup>
Modulus of Rigidity (G) (6061 Aluminum)		2.4E+10 N/m <sup>2</sup>	
Rotation Angle Per Stage (6061 Aluminum)	0.000448 degrees		7.81E-06 rad
Total Rotation (6061 Aluminum)	0.002239 degrees		3.91E-05 rad
Modulus of Rigidity (G) (304 Stainless Steel)		7.8E+10 N/m <sup>2</sup>	
Rotation Angle Per Stage (304 Stainless Steel)	0.000138 degrees		2.4E-06 rad
Total Rotation (304 Stainless Steel)	0.000689 degrees		1.2E-05 rad

these are guesses from [http://reprap.org/wiki/Stepper\\_torque](http://reprap.org/wiki/Stepper_torque) and <http://www.pbclinear.com/Download/DataSheet/Stepper-i>  
 this is set by the standard dimensions of a CFA.5" flange  
 this is probably thinner than would be used, but it gives conservative numbers

Stage Connection Key Slop	0.005 in		0.000127 m
Rotation From Each Key Slop	0.229183 degrees		0.004 rad
Total Key Slop Rotation	0.916732 degrees		0.016 rad
Total Rotation Of Shell (6061 Aluminum)	0.918971 degrees		0.016039 rad
Total Rotation Of Shell (304 Stainless Steel)	0.917421 degrees		0.016012 rad

If we imagine the keying between each stage of the shell to be a simple protrusion and recess system, there will be some rotational slop from that keying, primarily from dimensional differences in the fabrication





SS pin (17-4 PH)  
in ceramic bushings

